

# Math 2283 - Introduction to Logic

Quiz #13 - 2012.11.30

Solutions

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1. Described what a closed system consists of, and what the implications of a closed system are.

A closed system consists of a set of true conditional statements  $p_i \rightarrow q_i$ ,  $1 \leq i \leq n$ , where the antecedents (the  $p_i$ 's) are exhaustive, and the consequents (the  $q_i$ 's) are exclusive. In a closed system the converse statements  $q_i \rightarrow p_i$ ,  $1 \leq i \leq n$ , are also true.

2. Write down the definition of a binary operation  $O$  being monotonic in a class  $K$  with respect to the relation  $R$ .

$$\mathbf{A}_{x,y,z} y R z \rightarrow (x O y) R (x O z)$$