

# Math 2315 - Calculus 2

Final Exam - 2017.5.01

Name: \_\_\_\_\_

1. Compute the following integral:  $\int \cos(\ln(x)) dx$
2. Compute the following integral:  $\int w^3 \sqrt{9 - w^2} dw$
3. Compute the following integral:  $\int \frac{z + 1}{z^2 + 4z - 5} dz$
4. Find the exact value of the following sum:  $\sum_{k=1}^{\infty} \frac{1}{k(k+1)(k+2)}$
5. Determine if  $\sum_{k=1}^{\infty} \frac{(k!)^2}{(2k)!}$  converges or diverges.
6. Determine if  $\sum_{k=1}^{\infty} (1 - \cos(1/k))$  converges by comparing to the sum  $\sum_{k=1}^{\infty} \frac{1}{k^2}$ .
7. Define  $c_n = \frac{1}{n^2 + 1} + \frac{1}{n^2 + 2} + \cdots + \frac{1}{n^2 + n}$ . Show that for all  $n$ ,  $\frac{n}{n^2 + n} \leq c_n \leq \frac{n}{n^2 + 1}$ .
8. Using the result above from problem 7, determine if  $\{c_n\}_{n=1}^{\infty}$  converges, and if so, to what value.
9. Convert the polar coordinate  $(6, 3/4\pi)$  to rectangular coordinate form.
10. Convert  $(-6/\sqrt{2}, 6/\sqrt{2})$  to polar coordinate form, and give three distinct answers.
11. Plot the polar function  $r = 2 + 2 \cos(3\theta)$ , for  $0 \leq \theta \leq 2\pi$ .
12. Compute the tangent line to polar function  $r = 2 + 2 \cos(3\theta)$  at  $\theta = 2/3\pi$ .
13. Compute the interval of convergence for the power series:  $\sum_{k=0}^{\infty} \frac{(-1)^k x^k}{\sqrt{k^2 + 1}}$ .
14. Express the following integral as an infinite series:  $\int_0^x \frac{1 - \cos(t)}{t} dt$ .
15. Find the Maclaurin series for  $f(x) = x^2 e^{x^2}$ .
16. Plot the parametric function  $(x(t), y(t)) = (\cos(t) \sin(t), \sin(t))$ , for  $t \in [0, 2\pi]$ .
17. Find the exact value of the following sum:  $\sum_{k=2}^{\infty} 3 \left(\frac{4}{5}\right)^k$
18. Determine if the following series converges absolutely, conditionally, or diverges:  $\sum_{k=1}^{\infty} (-1)^k \frac{1}{\sqrt[3]{k} + 2k}$