

# Math 4982 - Senior Seminar Trigonometry Review Questions

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1. [10 pts] Fill out the following table completely:

$\theta^\circ$	$0^\circ$	$30^\circ$	$45^\circ$	$60^\circ$	$90^\circ$	$120^\circ$	$135^\circ$	$150^\circ$	$180^\circ$
$\theta$ (rad)									
$\sin(\theta)$									
$\cos(\theta)$									

2. Convert  $17^\circ 15'$  to decimal degrees.

3. Convert  $29.45^\circ$  to degrees, minutes, and seconds.

4. Convert  $625^\circ$  to radian measure.

5. Convert  $\frac{3}{17}\pi$  radians to degree measure.

6. If the area  $\mathcal{A}$  of the sector of a circle with central angle  $\theta = \frac{1}{2}$  radians is 100 square units, what is the radius of the circle?

7. Sketch the graph of  $f(x) = 2 \sin\left(\frac{2}{3}x - \frac{\pi}{2}\right) - 2$  over two full periods.

8. Sketch the graph of  $f(x) = \tan(3x + \pi) + 1$  over two full periods.

9. Sketch the graph of  $f(x) = \frac{1}{2} \sec\left(2x - \frac{\pi}{4}\right) + 1$  over two full periods.

10. Prove the following trigonometric identity:

$$\frac{\tan^3(t) - \cot^3(t)}{\tan(t) - \cot(t)} = \sec^2(t) + \cot^2(t)$$

11. Prove the following trigonometric identity:

$$\sin(\theta) + \cos(\theta) + 1 = \frac{2 \sin(\theta) \cos(\theta)}{\sin(\theta) + \cos(\theta) - 1}$$

12. Prove the following trigonometric identity:

$$\tan(A + B + C) = \frac{\tan(A) + \tan(B) + \tan(C) + \tan(A) \tan(B) \tan(C)}{1 + \tan(A) \tan(B) + \tan(A) \tan(C) + \tan(B) \tan(C)}$$

13. Prove the following trigonometric identity:

$$\frac{\cos(5w) + \cos(w)}{\cos(w) - \cos(5w)} = \frac{\cot(2w)}{\tan(3w)}$$

14. Compute exactly  $\tan\left(\frac{\pi}{8}\right)$ .

15. Find all solutions for  $0 \leq x < 2\pi$  to the equation:  $\sin(2x - 1) = \frac{1}{2}$ .

16. Find all solutions for  $0 \leq z < 2\pi$  to the equation:  $1 - \sin(z) = \cos(2z)$ .
17. Write  $\cos(2 \tan^{-1}(x))$  as an algebraic expression only, free of trigonometric or inverse trigonometric functions.
18. A triangle has corners given by the points  $(1, 2)$ ,  $(-1, 1)$ , and  $(-3, 4)$ . Graph this triangle in the  $xy$ -plane and use the vector approach to compute the cosine of each angle in the triangle. Remember  $\cos(\theta) = \frac{\vec{u} \cdot \vec{v}}{|\vec{u}||\vec{v}|}$ .
19. Given the vector  $\vec{u} = \langle 2, 3, -1, 1, 4 \rangle$ , find two nonzero vectors  $\vec{v}$  and  $\vec{w}$  which are perpendicular to  $\vec{u}$  such that  $\vec{v}$  and  $\vec{w}$  do not lie on the same line.